

A Complete Algorithm for Generating Landmarks

Blai Bonet Julio Castillo

Universidad Simón Bolívar, Caracas, Venezuela

ICAPS 2011 – Freiburg, June 2011

Introduction

- multiple uses of landmarks in planning
- most powerful admissible heuristics are based on landmarks
- we know . . .
 - a lot about **exploiting** landmarks
 - little about **generation** of landmarks
- this work is about generation of landmarks

Our contribution

- **principled** algorithm for generating landmarks
- landmarks can be used for different purposes
- a general framework for heuristics based on landmarks:
 - admissible for **optimal** planning
 - non-admissible for **satisficing** planning
- **polytime** admissible heuristic

Relaxed Planning

Obtained by **removing the deletes** of each action

Relaxed task characterized by:

- finite set F of **facts**
- initial facts $I \subseteq F$
- goal facts $G \subseteq F$ that must be reached
- operators of the form $o[4] : a, b \rightarrow c, d$
read: If we already have facts a and b (**preconditions** $pre(o)$),
we can apply o , paying 4 units (**cost** $cost(o)$),
to obtain facts c and d (**effects** $eff(o)$)

Assume WLOG: $I = \{i\}$, $G = \{g\}$, all $pre(o) \neq \emptyset$

Example

$o_1[3] : i \rightarrow a, b$

$o_2[4] : i \rightarrow a, c$

$o_3[5] : i \rightarrow b, c$

$o_4[1] : a, b \rightarrow d$

$o_5[1] : a, c, d \rightarrow g$

One way to reach goal $G = \{g\}$ from $I = \{i\}$:

- apply sequence o_1, o_2, o_4, o_5 (**plan**)
- cost: $3 + 4 + 1 + 1 = 9$ (**optimal**)

Optimal Relaxed Cost

- h^+ : minimal total cost to reach G from I
- **Very good heuristic** function for optimal planning
- **NP-hard** to compute or approximate by constant factor

Landmarks

Most accurate admissible heuristics are based on landmarks

Def: a (disjunctive action) landmark is a set of operators L such that each plan must contain some action in L

Example

$o_1[3] : i \rightarrow a, b$

$o_2[4] : i \rightarrow a, c$

$o_3[5] : i \rightarrow b, c$

$o_4[1] : a, b \rightarrow d$

$o_5[1] : a, d, c \rightarrow g$

Some landmarks:

- need g : $W = \{o_5\}$ (hence $h^+ \geq 1$)
- need a : $X = \{o_1, o_2\}$ (hence $h^+ \geq 3$)
- need c : $Y = \{o_2, o_3\}$ (hence $h^+ \geq 4$)
- need d : $Z = \{o_4\}$ (hence $h^+ \geq 1$)
- ...

Exploiting Landmarks: Hitting Sets

Given:

- finite set A
- collection \mathcal{F} of subsets from A
- non-negative costs $c : A \rightarrow \mathbb{R}_0^+$

Hitting set:

- subset $H \subseteq A$ that **hits** every $S \in \mathcal{F}$ (i.e. $S \cap H \neq \emptyset$)
- cost of $H = \sum_{a \in H} c(a)$

Minimum-cost Hitting Set (MHS):

- minimizes cost
- classical NP-complete problem

Landmarks and Hitting Sets

Can view **collection of landmarks** as instance of MHS problem

Example (Landmarks)

$$A = \{o_1, o_2, o_3, o_4, o_5\}$$

$$\mathcal{F} = \left\{ \underbrace{\{o_5\}}_W, \underbrace{\{o_1, o_2\}}_X, \underbrace{\{o_2, o_3\}}_Y, \underbrace{\{o_4\}}_Z \right\}$$

$$\text{costs: } c(o_1) = 3, \quad c(o_2) = 4, \quad c(o_3) = 5, \quad c(o_4) = 1, \quad c(o_5) = 1$$

Minimum hitting set: $\{o_2, o_4, o_5\}$ with cost $4 + 1 + 1 = 6$

Obtaining Landmarks: Justification Graphs

Precondition choice function (pcf): function D that maps operators to preconditions

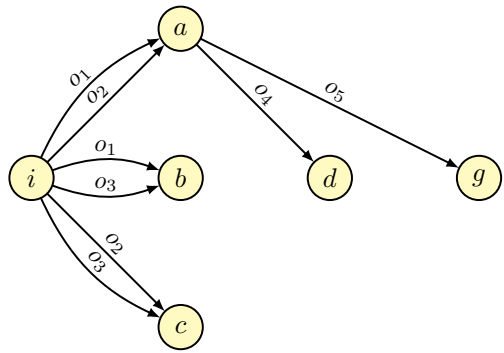
Justification graph for pcf D : arc-labeled digraph with:

- vertices: the facts F
- arcs: $D(o) \xrightarrow{o} e$ for each operator o and effect $e \in \text{eff}(o)$

pcf D :

o	o_1	o_2	o_3	o_4	o_5
$D(o)$	i	i	i	a	a

- $o_1[3] : i \rightarrow a, b$
- $o_2[4] : i \rightarrow a, c$
- $o_3[5] : i \rightarrow b, c$
- $o_4[1] : a, b \rightarrow d$
- $o_5[1] : a, c, d \rightarrow g$

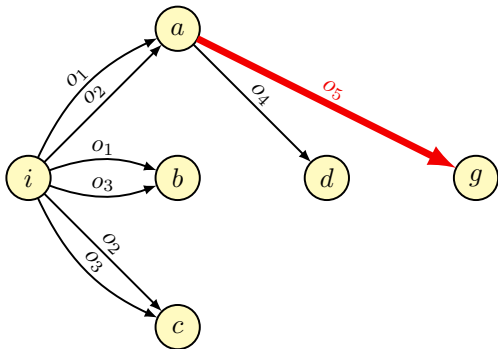


pcf D :

o	o_1	o_2	o_3	o_4	o_5
$D(o)$	i	i	i	a	a

Landmark (cut): $W = \{o_5\}$

- $o_1[3] : i \rightarrow a, b$
- $o_2[4] : i \rightarrow a, c$
- $o_3[5] : i \rightarrow b, c$
- $o_4[1] : a, b \rightarrow d$
- $o_5[1] : a, c, d \rightarrow g$

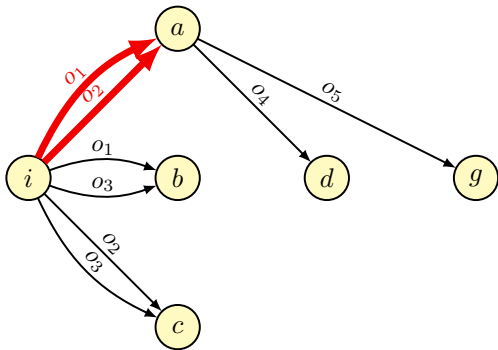


pcf D :

o	o_1	o_2	o_3	o_4	o_5
$D(o)$	i	i	i	a	a

Landmark (cut): $X = \{o_1, o_2\}$

- $o_1[3] : i \rightarrow a, b$
- $o_2[4] : i \rightarrow a, c$
- $o_3[5] : i \rightarrow b, c$
- $o_4[1] : a, b \rightarrow d$
- $o_5[1] : a, c, d \rightarrow g$



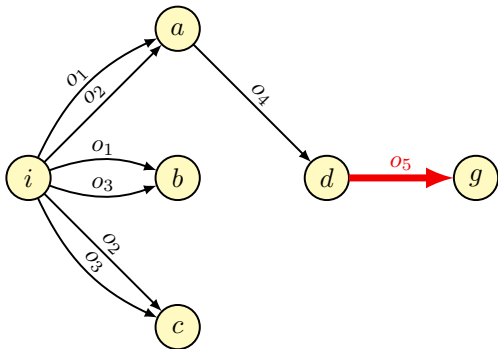
pcf D :

o	o_1	o_2	o_3	o_4	o_5
$D(o)$	i	i	i	a	d

(new pcf)

Landmark (cut): $W = \{o_5\}$

- $o_1[3] : i \rightarrow a, b$
- $o_2[4] : i \rightarrow a, c$
- $o_3[5] : i \rightarrow b, c$
- $o_4[1] : a, b \rightarrow d$
- $o_5[1] : a, c, d \rightarrow g$

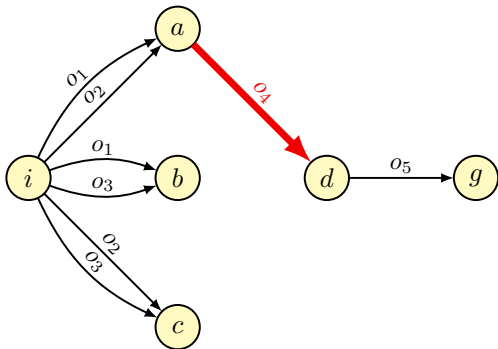


pcf D :

o	o_1	o_2	o_3	o_4	o_5
$D(o)$	i	i	i	a	d

Landmark (cut): $Z = \{o_4\}$

- $o_1[3] : i \rightarrow a, b$
- $o_2[4] : i \rightarrow a, c$
- $o_3[5] : i \rightarrow b, c$
- $o_4[1] : a, b \rightarrow d$
- $o_5[1] : a, c, d \rightarrow g$

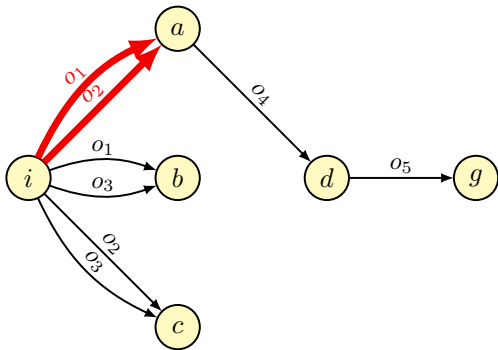


pcf D :

o	o_1	o_2	o_3	o_4	o_5
$D(o)$	i	i	i	a	d

Landmark (cut): $X = \{o_1, o_2\}$

- $o_1[3] : i \rightarrow a, b$
- $o_2[4] : i \rightarrow a, c$
- $o_3[5] : i \rightarrow b, c$
- $o_4[1] : a, b \rightarrow d$
- $o_5[1] : a, c, d \rightarrow g$



Power of Justification Graph Cuts

Thm (B. & Helmert, 2010): Let \mathcal{L} be all “cut landmarks”.
Then, $h^+ = \text{cost of MHS for } \mathcal{L}$.

Power of Justification Graph Cuts

Thm (B. & Helmert, 2010): Let \mathcal{L} be all “cut landmarks”.
Then, $h^+ = \text{cost of MHS for } \mathcal{L}$.

Impractical to generate all landmarks!

Do we need all of them to get h^+ or a good approximation?

Principled Generation of Landmarks

H = subset of operators

R = fluents reachable from I using only operators in H

H = subset of operators

R = **fluents reachable** from I using only operators in H

$g \in R \implies H$ **“contains”** a relaxed plan

$g \notin R \implies (R, R^c)$ is cut of **some** justification graph $G(D)$

and H **does not hit** cutset(R, R^c)

H = subset of operators

R = **fluents reachable** from I using only operators in H

$g \in R \implies H$ **"contains"** a relaxed plan

$g \notin R \implies (R, R^c)$ is cut of **some** justification graph $G(D)$

and H **does not hit** cutset(R, R^c)

Indeed, it's enough to define pcf D as $D(o) = p$ where

$$\begin{cases} p \in \text{pre}(o) & \text{if } \text{pre}(o) \subseteq R \\ p \in \text{pre}(o) \setminus R & \text{if } \text{pre}(o) \not\subseteq R \end{cases}$$

For such pcf D ,

$$L = \text{cutset}(R, R^c) = \{o : D(o) \in R \text{ and } \text{eff}(o) \notin R^c\}$$

is landmark not hit by H !

For such pcf D ,

$$L = \text{cutset}(R, R^c) = \{o : D(o) \in R \text{ and } \text{eff}(o) \not\subseteq R^c\}$$

is landmark not hit by H !

L improved by removing from $G(D)$ facts irrelevant to g

Algorithm A

Input: subset H of actions

Output: YES if H contains plan, or landmark not hit by H

Method:

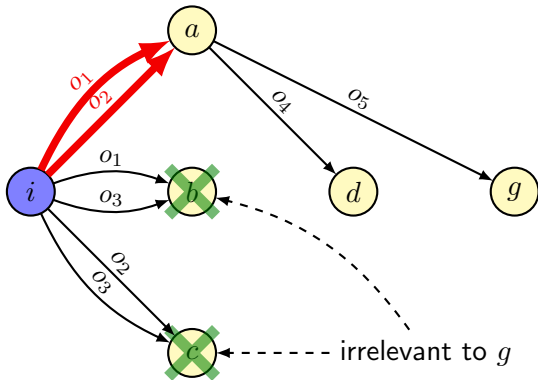
- 1 $R :=$ set of reachable fluents using actions in H
- 2 **if** $g \in H$ **then return** YES
- 3 compute pcf D and justification graph $G(D)$
- 4 simplify graph $G(D)$
- 5 **return** cutset of (R, R^c) in simplified graph

Time: linear with correct data structures!

Landmarks = \emptyset

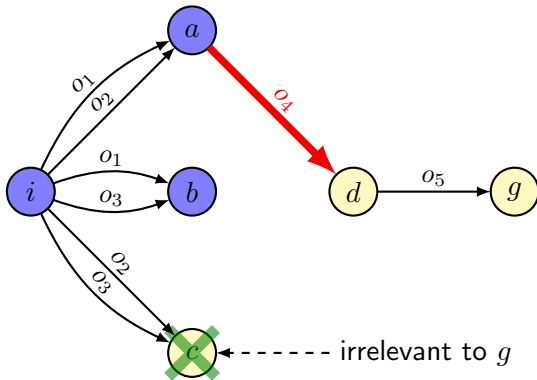
Landmarks = \emptyset

$H = \emptyset$; $R = \{i\}$; $R^c = \{a, b, c, d, g\}$; $L = \{o_1, o_2\}$



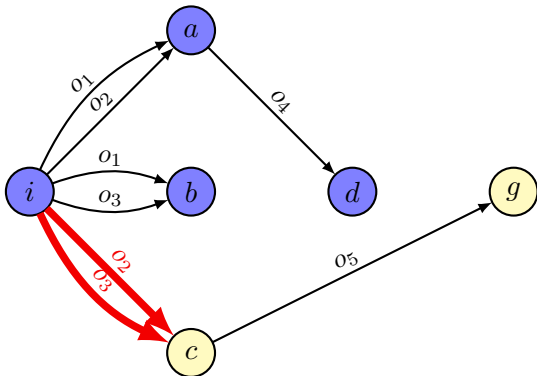
Landmarks = $\underbrace{\{\{o_1, o_2\}\}}_X$

$H = \{o_1\}$; $R = \{i, a, b\}$; $R^c = \{c, d, g\}$; $L = \{o_4\}$



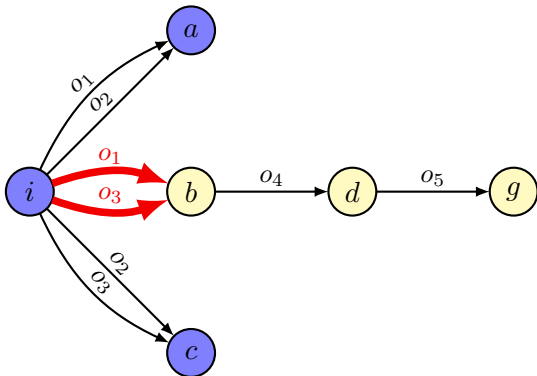
Landmarks = $\{\underbrace{\{o_1, o_2\}}_X, \underbrace{\{o_4\}}_Z\}$

$H = \{o_1, o_4\}$; $R = \{i, a, b, d\}$; $R^c = \{c, g\}$; $L = \{o_2, o_3\}$



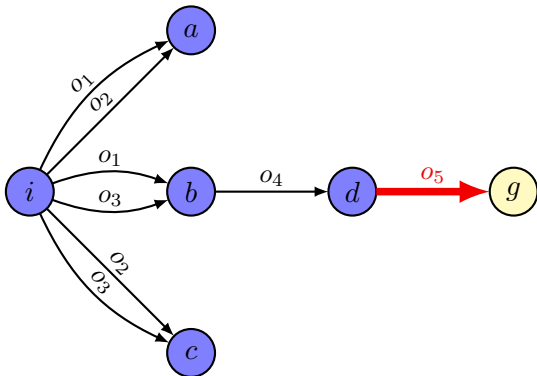
$$\text{Landmarks} = \underbrace{\{o_1, o_2\}}_X, \underbrace{\{o_4\}}_Z, \underbrace{\{o_2, o_3\}}_Y$$

$$H = \{o_2, o_4\} ; R = \{i, a, c\} ; R^c = \{b, g\} ; L = \{o_1, o_3\}$$



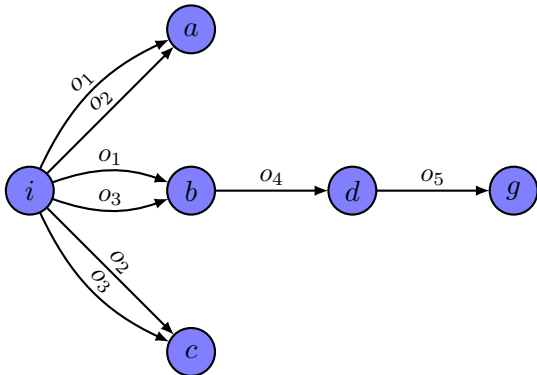
Landmarks = $\{\underbrace{\{o_1, o_2\}}_X, \underbrace{\{o_4\}}_Z, \underbrace{\{o_2, o_3\}}_Y, \{o_1, o_3\}\}$

$H = \{o_1, o_2, o_4\}$; $R = \{i, a, b, c, d\}$; $R^c = \{g\}$; $L = \{o_5\}$



Landmarks = $\underbrace{\{o_1, o_2\}}_X, \underbrace{\{o_4\}}_Z, \underbrace{\{o_2, o_3\}}_Y, \underbrace{\{o_1, o_3\}}_W, \underbrace{\{o_5\}}_W$ **complete!**

$H = \{o_1, o_2, o_4, o_5\}$; $R = \{i, a, b, c, d, g\}$; $R^c = \emptyset$



Algorithm $C1$

Input: initial collection \mathcal{L} (maybe empty)

Output: a complete collection and $h^+(I)$

Method:

- 1 $H :=$ min-cost hitting set for \mathcal{L}
- 2 $L := A(H)$
- 3 **if** $L = \text{YES}$ **then return** \mathcal{L} and cost of H
- 4 $\mathcal{L} := \mathcal{L} \cup \{L\}$
- 5 **goto** 2

Algorithm $C1$ **does not** run in polytime because:

- computing min-cost hitting sets is **NP-hard**
- number of iterations may be **exponential**

Flaws can be **overcomed** to get a polytime approximation by:

- controlling number of iterations
- controlling difficulty of solving MHS problem

See paper for:

- details about algorithm $C1$ and variants $C2$ and $C3$
- how to use A to get heuristics for **satisficing planning**
- novel polytime admissible heuristics that dominate best-known heuristics **(in number of expanded nodes)**

slower than state-of-the-art heuristics (i.e. LM-Cut)

Thanks!